## PROPOSED AMENDMENTS TO THE CLAIMS

RECEIVED CENTRAL FAX CENTER

JUN 2 0 2006

Claims 1-18 (Canceled)

19. (Currently Amended) A method of analyzing and computing modelling anisotropic turbulent flow of in an anisotropic fluid comprising:

providing input to a general purpose computer defining, for an anisotropic fluid, a set of moment equations governing time average thermal and turbulent motion, directional kinetic energy, shear, directional kinetic energy fluxes, and structure correlations;

instructing the general purpose computer to calculate  $n^{th}$  order, wherein n is odd, directional kinetic energy fluxes and structure correlation equations elosure relationships using  $(n+1)^{th}$  order density gradient independent time average thermal and turbulent moment closure relationships to yield a set of closed time average turbulent moment equations;

using the set of closed time average turbulent moment equations to predict anisotropic turbulent flow of the anisotropic fluid; and

calculating and displaying a turbulent flow quantity of physical importance;
wherein the set of moment equations governing time average turbulent directional
kinetic energy, shear, directional kinetic energy fluxes, and structure correlations is
defined by:

Directional Kinetic Turbulent Energy

$$\begin{split} &\frac{\partial}{\partial t} \left[ \overline{u_1'^2} \right] + \overline{u_1} \frac{\partial}{\partial x_1} \left[ \overline{u_1'^2} \right] + \overline{u_2} \frac{\partial}{\partial x_2} \left[ \overline{u_1'^2} \right] + \overline{u_3} \frac{\partial}{\partial x_3} \left[ \overline{u_1'^2} \right] \\ &+ 2 \left[ \overline{u_1'^2} \frac{\partial \overline{u_1}}{\partial x_1} + \overline{u_1'} \underline{u_2'} \frac{\partial \overline{u_1}}{\partial x_2} + \overline{u_1'} \underline{u_3'} \frac{\partial \overline{u_1}}{\partial x_3} \right] \\ &+ \frac{1}{\overline{\rho}} \left[ \frac{\partial}{\partial x_1} \left[ \overline{\rho} \overline{u_1'} \underline{u_1'^2} \right] + \frac{\partial}{\partial x_2} \left[ \overline{\rho} \overline{u_2'} \underline{u_1'^2} \right] + \frac{\partial}{\partial x_3} \left[ \overline{\rho} \overline{u_3'} \underline{u_1'^2} \right] \right] \\ &= 0 \end{split}$$

Turbulent-Shear

$$\begin{split} &\frac{\partial}{\partial t} \left[ \overline{u_1' u_2'} \right] + \overline{u_1} \frac{\partial}{\partial x_1} \left[ \overline{u_1' u_2'} \right] + \overline{u_2} \frac{\partial}{\partial x_2} \left[ \overline{u_1' u_2'} \right] + \overline{u_3} \frac{\partial}{\partial x_3} \left[ \overline{u_1' u_2'} \right] \\ &+ \overline{u_1' u_2'} \frac{\partial \overline{u_1}}{\partial x_1} + \overline{u_2'^2} \frac{\partial \overline{u_1}}{\partial x_2} + \overline{u_2' u_3'} \frac{\partial \overline{u_1}}{\partial x_3} \\ &+ \overline{u_1'^2} \frac{\partial \overline{u_2}}{\partial x_1} + \overline{u_1' u_2'} \frac{\partial \overline{u_2}}{\partial x_2} + \overline{u_1' u_3'} \frac{\partial \overline{u_2}}{\partial x_3} \\ &+ \frac{1}{\overline{\rho}} \left[ \frac{\partial}{\partial x_1} \left[ \overline{\rho} \overline{u_2' u_1'^2} \right] + \frac{\partial}{\partial x_2} \left[ \overline{\rho} \overline{u_1' u_2'^2} \right] + \frac{\partial}{\partial x_3} \left[ \overline{\rho} \overline{u_1' u_2' u_3'} \right] \right] \\ &= 0 \end{split}$$

Directional Kinetic Turbulent Energy Fluxes

$$\begin{split} &\frac{\partial}{\partial t} \left[ \overline{u_1' u_1'^2} \right] + \overline{u_1} \frac{\partial}{\partial x_1} \left[ \overline{u_1' u_1'^2} \right] + \overline{u_2} \frac{\partial}{\partial x_2} \left[ \overline{u_1' u_1'^2} \right] + \overline{u_3} \frac{\partial}{\partial x_3} \left[ \overline{u_1' u_1'^2} \right] \\ &+ 3 \left[ \overline{u_1' u_1'^2} \frac{\partial \overline{u_1}}{\partial x_1} + \overline{u_2' u_1'^2} \frac{\partial \overline{u_1}}{\partial x_2} + \overline{u_3' u_1'^2} \frac{\partial \overline{u_1}}{\partial x_3} \right] \\ &- 3 \overline{u_1'^2} \left[ \frac{\partial}{\partial x_1} \left[ \overline{u_1'^2} \right] + \frac{\partial}{\partial x_2} \left[ \overline{u_1' u_2'} \right] + \frac{\partial}{\partial x_3} \left[ \overline{u_1' u_3'} \right] \right] \\ &+ 3 \overline{\overline{c_1}^2} \left[ \frac{\delta}{\partial x_1} \left[ \overline{u_1'^2} \right] + \frac{\partial}{\partial x_2} \left[ \overline{u_1' u_2'} \right] + \frac{\partial}{\partial x_3} \left[ \overline{u_1' u_3'} \right] \right] \\ &+ 3 \left[ \overline{u_1'^2} \frac{\partial}{\partial x_1} \left[ \overline{\overline{c_1}^2} \right] + \overline{u_1' u_2'} \frac{\partial}{\partial x_2} \left[ \overline{\overline{c_1}^2} \right] + \overline{u_1' u_3'} \frac{\partial}{\partial x_3} \left[ \overline{\overline{c_1}^2} \right] \right] \\ &+ \frac{\partial}{\partial x_1} \left[ \overline{u_1'^2 u_1'^2} \right] + \frac{\partial}{\partial x_2} \left[ \overline{u_1' u_2' u_1'^2} \right] + \frac{\partial}{\partial x_3} \left[ \overline{u_1' u_3' u_1'^2} \right] \\ &+ \left[ \overline{u_1' u_2' u_1'^2} - 3 \overline{u_1' u_2'} \left[ \overline{u_1'^2} \right] \right] \frac{1}{\overline{\rho}} \frac{\partial \overline{\rho}}{\partial x_1} \\ &+ \left[ \overline{u_1' u_2' u_1'^2} - 3 \overline{u_1' u_2'} \left[ \overline{u_1'^2} \right] \right] \frac{1}{\overline{\rho}} \frac{\partial \overline{\rho}}{\partial x_2} \\ &+ \left[ \overline{u_1' u_2' u_1'^2} - 3 \overline{u_1' u_2'} \left[ \overline{u_1'^2} \right] \right] \frac{1}{\overline{\rho}} \frac{\partial \overline{\rho}}{\partial x_3} \\ &= 0 \end{aligned}$$

and

## Directional-Turbulent-Energy-Fluxes

310 820 5270

$$\begin{split} &\frac{\partial}{\partial t} \left[ \overline{u_1' u_2' u_3'} \right] + \overline{u_1} \frac{\partial}{\partial x_1} \left[ \overline{u_1' u_2' u_3'} \right] + \overline{u_2} \frac{\partial}{\partial x_2} \left[ \overline{u_1' u_2' u_3'} \right] + \overline{u_3} \frac{\partial}{\partial x_3} \left[ \overline{u_1' u_2' u_3'} \right] \\ &+ \overline{u_1' u_2' u_3'} \frac{\partial \overline{u_1}}{\partial x_1} + \overline{u_1' u_2' u_3'} \frac{\partial \overline{u_2}}{\partial x_2} + \overline{u_1' u_3' u_3'} \frac{\partial \overline{u_1}}{\partial x_3} \\ &+ \overline{u_2' u_1'^2} \frac{\partial \overline{u_2}}{\partial x_1} + \overline{u_1' u_2' u_3'} \frac{\partial \overline{u_2}}{\partial x_2} + \overline{u_1' u_3' u_3'} \frac{\partial \overline{u_2}}{\partial x_3} \\ &+ \overline{u_2' u_1'^2} \frac{\partial \overline{u_2}}{\partial x_1} + \overline{u_1' u_2' u_3'} \frac{\partial \overline{u_2}}{\partial x_2} + \overline{u_1' u_2' u_3'} \frac{\partial \overline{u_2}}{\partial x_3} \\ &- \overline{u_1' u_2'} \left[ \frac{\partial}{\partial x_1} \left[ \overline{u_1' u_2'} \right] + \frac{\partial}{\partial x_2} \left[ \overline{u_2' u_3'} \right] + \frac{\partial}{\partial x_3} \left[ \overline{u_2' u_3'} \right] \right] \\ &- \overline{u_1' u_3'} \left[ \frac{\partial}{\partial x_1} \left[ \overline{u_1' u_2'} \right] + \frac{\partial}{\partial x_2} \left[ \overline{u_1' u_2'} \right] + \frac{\partial}{\partial x_3} \left[ \overline{u_1' u_3'} \right] \right] \\ &+ \overline{u_1' u_3'} \frac{\partial}{\partial x_1} \left[ \overline{\overline{c_1 c_3}} \right] + \overline{u_1' u_2'} \frac{\partial}{\partial x_2} \left[ \overline{\overline{c_1 c_2}} \right] + \overline{u_1' u_3'} \frac{\partial}{\partial x_3} \left[ \overline{\overline{c_1 c_2}} \right] \\ &+ \overline{u_1' u_2'} \frac{\partial}{\partial x_1} \left[ \overline{\overline{c_1 c_2}} \right] + \overline{u_2' u_3'} \frac{\partial}{\partial x_2} \left[ \overline{\overline{c_1 c_2}} \right] + \overline{u_1' u_3'} \frac{\partial}{\partial x_3} \left[ \overline{\overline{c_1 c_2}} \right] \\ &+ \overline{c_1' u_3'} \frac{\partial}{\partial x_1} \left[ \overline{u_1' u_2'} \right] + \overline{c_1 c_2} \frac{\partial}{\partial x_2} \left[ \overline{u_1' u_2'} \right] + \overline{c_1 c_3} \frac{\partial}{\partial x_3} \left[ \overline{u_1' u_2'} \right] \\ &+ \overline{c_1 c_2} \frac{\partial}{\partial x_1} \left[ \overline{u_1' u_2'} \right] + \overline{c_2 c_3} \frac{\partial}{\partial x_2} \left[ \overline{u_1' u_2'} \right] + \overline{c_1 c_3} \frac{\partial}{\partial x_3} \left[ \overline{u_1' u_2'} \right] \\ &+ \overline{c_1 c_2} \frac{\partial}{\partial x_1} \left[ \overline{u_1' u_2'} \right] + \overline{c_2 c_3} \frac{\partial}{\partial x_2} \left[ \overline{u_1' u_2'} \right] + \overline{c_2 c_3} \frac{\partial}{\partial x_3} \left[ \overline{u_1' u_2'} \right] \\ &+ \overline{c_1 c_2} \frac{\partial}{\partial x_1} \left[ \overline{u_1' u_2'} \right] + \overline{c_2 c_3} \frac{\partial}{\partial x_2} \left[ \overline{u_1' u_2'} \right] + \overline{c_2 c_3} \frac{\partial}{\partial x_3} \left[ \overline{u_1' u_2'} \right] \\ &+ \overline{u_1' u_2' u_3' u_1'^2} - \overline{u_1' u_2'} \left[ \overline{u_1' u_2'} \right] - 2 \overline{u_1' u_2'} \left[ \overline{u_1' u_2'} \right] \right] \frac{\partial}{\partial} \frac{\partial}{\partial x_3} \\ &+ \left[ \overline{u_1' u_2' u_3'^2} - \overline{u_1' u_2'} \left[ \overline{u_1' u_2'} \right] - 2 \overline{u_1' u_2'} \left[ \overline{u_1' u_2'} \right] \right] \frac{\partial}{\partial} \frac{\partial}{\partial x_3} \\ &+ \left[ \overline{u_1' u_2' u_3'^2} - \overline{u_1' u_2'} \left[ \overline{u_1' u_2'} \right] - 2 \overline{u_1' u_2'} \left[ \overline{u_2' u_3'} \right] \right] \frac{\partial}{\partial} \frac{\partial}{\partial} \\ &+ \overline{u_1' u_2' u_3'^2} - \overline{u_1' u_2'} \left[ \overline{u_1' u_2'} \right] - 2 \overline{u_1' u_2'} \left[ \overline{u_1'$$

20. (Currently Amended) A computer readable storage medium containing a set of instructions for a general purpose computer, the set of instructions defining a method of deriving a set of closed time average turbulent moment equations for analyzing and computing modelling anisotropic turbulent flow of an anisotropic fluid comprising:

defining, for an anisotropic fluid, a set of moment equations governing time average thermal and turbulent motion, directional kinetic energy, shear, directional kinetic energy fluxes, and structure correlations;

calculating  $n^{th}$  order, wherein n is odd, directional kinetic energy fluxes and structure correlation equations elosure relationships using  $(n + 1)^{th}$  order density gradient independent time average thermal and turbulent moment closure relationships to yield a set of closed time average turbulent moment equations;

using the set of closed time average turbulent moment equations to predict anisotropic turbulent flow of the anisotropic fluid; and calculating and displaying a turbulent flow quantity of physical importance; wherein the set of moment equations governing time average turbulent directional kinetic energy, shear, directional kinetic energy fluxes, and structure correlations is defined by:

Directional Kinetic Turbulent Energy

$$\frac{\partial}{\partial t} \left[ \overline{u_1'^2} \right] + \overline{u_1} \frac{\partial}{\partial x_1} \left[ \overline{u_1'^2} \right] + \overline{u_2} \frac{\partial}{\partial x_2} \left[ \overline{u_1'^2} \right] + \overline{u_3} \frac{\partial}{\partial x_3} \left[ \overline{u_1'^2} \right] 
+ 2 \left[ \overline{u_1'^2} \frac{\partial \overline{u_1}}{\partial x_1} + \overline{u_1' u_2'} \frac{\partial \overline{u_1}}{\partial x_2} + \overline{u_1' u_3'} \frac{\partial \overline{u_1}}{\partial x_3} \right] 
+ \frac{1}{\overline{\rho}} \left[ \frac{\partial}{\partial x_1} \left[ \overline{\rho} \overline{u_1' u_1'^2} \right] + \frac{\partial}{\partial x_2} \left[ \overline{\rho} \overline{u_2' u_1'^2} \right] + \frac{\partial}{\partial x_3} \left[ \overline{\rho} \overline{u_3' u_1'^2} \right] \right] 
= 0$$

and

Turbulent-Shear

$$\begin{split} &\frac{\partial}{\partial t} \left[ \overline{u_1' u_2'} \right] + \overline{u_1} \frac{\partial}{\partial x_1} \left[ \overline{u_1' u_2'} \right] + \overline{u_2} \frac{\partial}{\partial x_2} \left[ \overline{u_1' u_2'} \right] + \overline{u_3} \frac{\partial}{\partial x_3} \left[ \overline{u_1' u_2'} \right] \\ &+ \overline{u_1' u_2'} \frac{\partial \overline{u_1}}{\partial x_1} + \overline{u_2'^2} \frac{\partial \overline{u_1}}{\partial x_2} + \overline{u_2' u_3'} \frac{\partial \overline{u_1}}{\partial x_3} \\ &+ \overline{u_1'^2} \frac{\partial \overline{u_2}}{\partial x_1} + \overline{u_1' u_2'} \frac{\partial \overline{u_2}}{\partial x_2} + \overline{u_1' u_3'} \frac{\partial \overline{u_2}}{\partial x_3} \\ &+ \frac{1}{\overline{\rho}} \left[ \frac{\partial}{\partial x_1} \left[ \overline{\rho} \overline{u_2' u_1'^2} \right] + \frac{\partial}{\partial x_2} \left[ \overline{\rho} \overline{u_1' u_2'^2} \right] + \frac{\partial}{\partial x_3} \left[ \overline{\rho} \overline{u_1' u_2' u_3'} \right] \right] \\ &= 0 \end{split}$$

Directional Kinetic Turbulent Energy Fluxes

$$\frac{\partial}{\partial t} \left[ \overline{u_{1}' u_{1}'^{2}} \right] + \overline{u_{1}} \frac{\partial}{\partial x_{1}} \left[ \overline{u_{1}' u_{1}'^{2}} \right] + \overline{u_{2}} \frac{\partial}{\partial x_{2}} \left[ \overline{u_{1}' u_{1}'^{2}} \right] + \overline{u_{3}} \frac{\partial}{\partial x_{3}} \left[ \overline{u_{1}' u_{1}'^{2}} \right]$$

$$+ 3 \left[ \overline{u_{1}' u_{1}'^{2}} \frac{\partial \overline{u_{1}}}{\partial x_{1}} + \overline{u_{2}' u_{1}'^{2}} \frac{\partial \overline{u_{1}}}{\partial x_{2}} + \overline{u_{3}' u_{1}'^{2}} \frac{\partial \overline{u_{1}}}{\partial x_{3}} \right]$$

$$- 3 \overline{u_{1}'^{2}} \left[ \frac{\partial}{\partial x_{1}} \left[ \overline{u_{1}'^{2}} \right] + \frac{\partial}{\partial x_{2}} \left[ \overline{u_{1}' u_{2}'} \right] + \frac{\partial}{\partial x_{3}} \left[ \overline{u_{1}' u_{2}'} \right] \right]$$

$$+ 3 \overline{\overline{c_{1}^{2}}} \left[ \frac{\partial}{\partial x_{1}} \left[ \overline{u_{1}'^{2}} \right] + \frac{\partial}{\partial x_{2}} \left[ \overline{u_{1}' u_{2}'} \right] + \frac{\partial}{\partial x_{3}} \left[ \overline{u_{1}' u_{3}'} \right] \right]$$

$$+ 3 \left[ \overline{u_{1}'^{2}} \frac{\partial}{\partial x_{1}} \left[ \overline{\overline{c_{1}^{2}}} \right] + \overline{u_{1}' u_{2}'} \frac{\partial}{\partial x_{2}} \left[ \overline{\overline{c_{1}^{2}}} \right] + \overline{u_{1}' u_{3}'} \frac{\partial}{\partial x_{3}} \left[ \overline{\overline{c_{1}^{2}}} \right] \right]$$

$$+ \frac{\partial}{\partial x_{1}} \left[ \overline{u_{1}'^{2} u_{1}'^{2}} \right] + \frac{\partial}{\partial x_{2}} \left[ \overline{u_{1}' u_{2}' u_{1}'^{2}} \right] + \frac{\partial}{\partial x_{3}} \left[ \overline{u_{1}' u_{3}' u_{1}'^{2}} \right]$$

$$+ \left[ \overline{u_{1}'' u_{2}' u_{1}'^{2}} - 3 \overline{u_{1}' u_{2}'} \left[ \overline{u_{1}'^{2}} \right] \right] \frac{1}{\overline{\rho}} \frac{\partial \overline{\rho}}{\partial x_{2}}$$

$$+ \left[ \overline{u_{1}' u_{2}' u_{1}'^{2}} - 3 \overline{u_{1}' u_{3}'} \left[ \overline{u_{1}'^{2}} \right] \frac{1}{\overline{\rho}} \frac{\partial \overline{\rho}}{\partial x_{3}}$$

$$= 0$$

## Directional Turbulent Energy Fluxes

$$\begin{split} &\frac{\partial}{\partial t} \left[ \overline{u_1' u_2'^2} \right] + \overline{u_2} \frac{\partial}{\partial x_2} \left[ \overline{u_1' u_2'^2} \right] + \overline{u_1} \frac{\partial}{\partial x_1} \left[ \overline{u_1' u_2'^2} \right] + \overline{u_3} \frac{\partial}{\partial x_3} \left[ \overline{u_1' u_2'^2} \right] \\ &+ 2 \left[ \overline{u_1' u_2'^2} \frac{\partial \overline{u_2}}{\partial x_2} + \overline{u_2' u_1'^2} \frac{\partial \overline{u_2}}{\partial x_1} + \overline{u_1' u_2' u_3'} \frac{\partial \overline{u_2}}{\partial x_3} \right] \\ &+ \overline{u_2' u_2'^2} \frac{\partial \overline{u_1}}{\partial x_1} + \overline{u_1' u_1'^2} \frac{\partial \overline{u_1}}{\partial x_1} + \overline{u_3' u_1'^2} \frac{\partial \overline{u_1}}{\partial x_3} \\ &- 2 \overline{u_1' u_2'} \left[ \frac{\partial}{\partial x_2} \left[ \overline{u_1' u_2'} \right] + \frac{\partial}{\partial x_1} \left[ \overline{u_1' u_2'} \right] + \frac{\partial}{\partial x_3} \left[ \overline{u_1' u_3'} \right] \right] \\ &- \overline{u_2'^2} \left[ \frac{\partial}{\partial x_2} \left[ \overline{u_1' u_2'} \right] + \overline{\overline{c_1 \overline{c_2}}} \frac{\partial}{\partial x_1} \left[ \overline{u_1' u_2'} \right] + \overline{\overline{c_1 \overline{c_2}}} \frac{\partial}{\partial x_3} \left[ \overline{u_1' u_3'} \right] \right] \\ &+ 2 \left[ \overline{\overline{c_2'}} \frac{\partial}{\partial x_2} \left[ \overline{u_1' u_2'} \right] + \overline{\overline{c_1 \overline{c_2}}} \frac{\partial}{\partial x_1} \left[ \overline{u_1' u_2'} \right] + \overline{\overline{c_1 \overline{c_3}}} \frac{\partial}{\partial x_3} \left[ \overline{u_1' u_2'} \right] \right] \\ &+ 2 \left[ \overline{u_1'^2} \frac{\partial}{\partial x_2} \left[ \overline{u_1' u_2'} \right] + \overline{\overline{c_1'^2}} \frac{\partial}{\partial x_1} \left[ \overline{u_1' u_2'} \right] + \overline{\overline{c_1 \overline{c_3}}} \frac{\partial}{\partial x_3} \left[ \overline{u_1' u_2'} \right] \right] \\ &+ 2 \left[ \overline{u_1' u_2'} \frac{\partial}{\partial x_2} \left[ \overline{u_1' u_2'} \right] + \overline{u_1' u_2'} \frac{\partial}{\partial x_1} \left[ \overline{u_1' u_2'} \right] + \overline{u_1' u_2'} \frac{\partial}{\partial x_3} \left[ \overline{u_1' u_2'} \right] \right] \\ &+ 2 \left[ \overline{u_1' u_2' u_2'^2} \right] + \overline{u_1' u_2'} \frac{\partial}{\partial x_1} \left[ \overline{\overline{c_2'}} \right] + \overline{u_1' u_2'} \frac{\partial}{\partial x_1} \left[ \overline{u_1' u_2'} \right] \right] \\ &+ 2 \left[ \overline{u_1' u_2' u_2'^2} \right] + \overline{u_1' u_2'} \frac{\partial}{\partial x_1} \left[ \overline{\overline{c_2'}} \right] + \overline{u_1' u_2'} \frac{\partial}{\partial x_3} \left[ \overline{u_1' u_2'} \right] \right] \\ &+ 2 \left[ \overline{u_1' u_2' u_2'^2} \right] + \overline{u_1' u_2'} \frac{\partial}{\partial x_1} \left[ \overline{u_1'^2 u_2'^2} \right] + \overline{u_1' u_2'} \frac{\partial}{\partial x_3} \left[ \overline{u_1' u_2'} \right] \right] \\ &+ 2 \left[ \overline{u_1' u_2' u_2'^2} \right] + \overline{u_1' u_2'} \frac{\partial}{\partial x_2} \left[ \overline{u_1' u_2'} \right] \left[ \overline{u_1' u_2'} \right] \right] \\ &+ 2 \left[ \overline{u_1' u_2' u_2'^2} \right] + \overline{u_1' u_2'} \frac{\partial}{\partial x_3} \left[ \overline{u_1' u_2'} \right] \right] \\ &+ 2 \left[ \overline{u_1' u_2' u_2'^2} \right] + \overline{u_1' u_2'} \frac{\partial}{\partial x_3} \left[ \overline{u_1' u_2'} \right] \right] \\ &+ 2 \left[ \overline{u_1' u_2' u_2'^2} \right] + \overline{u_1' u_2'} \frac{\partial}{\partial x_3} \left[ \overline{u_1' u_2' u_2'^2} \right] \\ &+ 2 \left[ \overline{u_1' u_2' u_2'^2} \right] + \overline{u_1' u_2'} \frac{\partial}{\partial x_3} \left[ \overline{u_1' u_2' u_2'^2} \right] \\ &+ 2 \left[ \overline{u_1' u_2' u_2' u_2'^2} \right] + \overline{u_1' u_2' u_2'^2} \right] \\ &+ 2 \left[ \overline{u_1' u_2' u_2' u_2'^2} \right]$$

## Structure Correlations

$$\begin{split} &\frac{\partial}{\partial t} \left[ \overline{u_1' u_2' u_3'} \right] + \overline{u_1} \frac{\partial}{\partial x_1} \left[ \overline{u_1' u_2' u_3'} \right] + \overline{u_2} \frac{\partial}{\partial x_2} \left[ \overline{u_1' u_2' u_3'} \right] + \overline{u_3} \frac{\partial}{\partial x_3} \left[ \overline{u_1' u_2' u_3'} \right] \\ &+ \overline{u_1' u_2' u_3'} \frac{\partial \overline{u_1}}{\partial x_1} + \overline{u_1' u_2' u_3'} \frac{\partial \overline{u_2}}{\partial x_2} + \overline{u_1' u_3'} \frac{\partial \overline{u_2}}{\partial x_3} \\ &+ \overline{u_2' u_1'^2} \frac{\partial \overline{u_2}}{\partial x_1} + \overline{u_1' u_2'^2} \frac{\partial \overline{u_2}}{\partial x_3} + \overline{u_1' u_2' u_3'} \frac{\partial \overline{u_2}}{\partial x_3} \\ &+ \overline{u_2' u_1'^2} \frac{\partial \overline{u_2}}{\partial x_1} + \overline{u_1' u_2'^2} \frac{\partial \overline{u_2}}{\partial x_3} + \overline{u_1' u_2' u_3'} \frac{\partial \overline{u_2}}{\partial x_3} \\ &- \overline{u_1' u_2'} \left[ \frac{\partial}{\partial x_1} \left[ \overline{u_1' u_2'} \right] + \frac{\partial}{\partial x_2} \left[ \overline{u_2' u_3'} \right] + \frac{\partial}{\partial x_3} \left[ \overline{u_2' u_3'} \right] \right] \\ &- \overline{u_1' u_3'} \left[ \frac{\partial}{\partial x_1} \left[ \overline{u_1' u_2'} \right] + \frac{\partial}{\partial x_2} \left[ \overline{u_1' u_2'} \right] + \frac{\partial}{\partial x_3} \left[ \overline{u_1' u_3'} \right] \right] \\ &+ \overline{u_1' u_3'} \frac{\partial}{\partial x_1} \left[ \overline{c_1 \overline{c_2}} \right] + \overline{u_1' u_2'} \frac{\partial}{\partial x_2} \left[ \overline{c_1 \overline{c_2}} \right] + \overline{u_1' u_3'} \frac{\partial}{\partial x_2} \left[ \overline{c_1 \overline{c_2}} \right] \\ &+ \overline{u_1' u_3'} \frac{\partial}{\partial x_1} \left[ \overline{c_1 \overline{c_2}} \right] + \overline{u_2' u_3'} \frac{\partial}{\partial x_2} \left[ \overline{c_1 \overline{c_2}} \right] + \overline{u_2' u_3'} \frac{\partial}{\partial x_3} \left[ \overline{u_1' u_3'} \right] \\ &+ \overline{c_1''} \frac{\partial}{\partial x_1} \left[ \overline{u_1' u_2'} \right] + \overline{c_2' c_3} \frac{\partial}{\partial x_2} \left[ \overline{u_1' u_2'} \right] + \overline{c_3''} \frac{\partial}{\partial x_3} \left[ \overline{u_1' u_3'} \right] \\ &+ \overline{c_1 \overline{c_3}} \frac{\partial}{\partial x_1} \left[ \overline{u_1' u_2'} \right] + \overline{c_2 \overline{c_3}} \frac{\partial}{\partial x_2} \left[ \overline{u_1' u_2'} \right] + \overline{c_3''} \frac{\partial}{\partial x_3} \left[ \overline{u_1' u_3'} \right] \\ &+ \overline{c_1 \overline{c_3}} \frac{\partial}{\partial x_1} \left[ \overline{u_1' u_2'} \right] + \overline{c_2 \overline{c_3}} \frac{\partial}{\partial x_2} \left[ \overline{u_1' u_2'} \right] + \overline{c_3''} \frac{\partial}{\partial x_3} \left[ \overline{u_1' u_2'} \right] \\ &+ \overline{c_1 \overline{c_3}} \frac{\partial}{\partial x_1} \left[ \overline{u_1' u_2'} \right] + \overline{c_2''} \frac{\partial}{\partial x_2} \left[ \overline{u_1' u_2'} \right] + \overline{c_3''} \frac{\partial}{\partial x_3} \left[ \overline{u_1' u_2'} \right] \\ &+ \overline{c_1 \overline{c_3}} \frac{\partial}{\partial x_1} \left[ \overline{u_1' u_2'} \right] + \overline{c_2''} \frac{\partial}{\partial x_2} \left[ \overline{u_1' u_2'} \right] + \overline{c_3''} \frac{\partial}{\partial x_3} \left[ \overline{u_1' u_2'} \right] \\ &+ \overline{c_1 \overline{c_3}} \frac{\partial}{\partial x_1} \left[ \overline{u_1' u_2'} \right] + \overline{c_2''} \frac{\partial}{\partial x_2} \left[ \overline{u_1' u_2'} \right] + \overline{c_3''} \frac{\partial}{\partial x_3} \left[ \overline{u_1' u_2'} \right] \\ &+ \overline{c_1 \overline{c_3}} \frac{\partial}{\partial x_1} \left[ \overline{u_1' u_2'} \right] + \overline{c_2''} \frac{\partial}{\partial x_2} \left[ \overline{u_1' u_2'} \right] - 2 \overline{u_1' u_2'} \left[ \overline{u_1' u_2'} \right] \right] \frac{\partial}{\partial x_3} \frac{\partial}{\partial x_3}$$